feynMF: Drawing Feynman Diagrams with LAT_EX and METAFONT*

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Abstract

feynMF is a IAT_EX package for easy drawing of professional quality Feynman diagrams with METAFONT (or METAPOST). feynMF lays out most diagrams satisfactorily from the structure of the graph without any need for manual intervention. Nevertheless all the power of METAFONT (or METAPOST) is available for obscure cases.

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Contents

1	Intr	oducti	on					4
	1.1	Purpos	se and scope					. 4
	1.2	Relatio	on to similar packages					. 5
	1.3	Histori	ical note					. 6
	1.4	Archite	ecture					. 6
	1.5	Conclu	sion			•	• •	. 6
2	Usa	ge						8
	2.1		package and environments					. 8
	2.2		ary files					
	2.3							
	2.4	The fe	ynmf perl script					. 12
	2.5		mode					
		2.5.1	External vertices					
		2.5.2	Arcs and internal vertices					
		2.5.3	Polygons					
		2.5.4	Color					
		2.5.5	Examples					
		2.5.6	Labels					
		2.5.7	Manipulating the layout					
		2.5.8	Skeletons					
		2.5.9	Pulling strings					
	2.6	Miscel	laneous commands					
		2.6.1	Graphs in graphs					
		2.6.2	Reusing diagrams					
		2.6.3	Grouping					
		2.6.4	Changing parameters					
		2.6.5	Shrinking					
		2.6.6	Debugging					
		2.6.7	Multiple vertices and arcs					
	2.7		liate mode					
		2.7.1	Arcs					
		2.7.2	Vertices					
		2.7.3	Declarations					
		2.7.4	Assignments					
		2.7.5	Examples					
	2.8		1ETAFONT					
	2.0	2.8.1	Extending feynMF					
	2.9		on traps, trouble shooting and frequently asked					
		(FAQs						
		2.9.1	Yalue is too large					
		2.9.2	Diagrams in the document are never updated					
		2.9.3	Disgrams show up in the wrong spot					
		2.9.4	Spurious labels show up					
	2.10		1 bugs					
	2.10	2.10.1	Chaotic manual					
			Delayed error messages					
		2.10.2	Multiple tadpoles	• •	•	•	•••	. 41
		2.10.0	maniple mappins	• •	•	•	• •	· 11

2.10.4	Hard limits																											41	L
--------	-------------	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	----	---

1 Introduction

1.1 Purpose and scope

In recent years, $T_E X^1$ [1] and $I_e^A T_E X^2$ [2] have revolutionized the way we share information in theoretical physics (and other areas). Not only does $T_E X$ provide typographical capabilities, which transcend those of commercial "wordprocessors" substantially, $T_E X$ documents are also completely portable. Since implementations are available on essentially all computers in use in the community, documents can be shared without the usual restrictions of proprietary data formats. This has enabled us to collaborate on papers with colleagues on the other side of the globe, to replace the mailing of hard copy preprints by electronic transmission and to submit these papers electronically to the publisher.

This portability comes with a price, though. T_EX (and LAT_EX) do not address the issue of graphical information, apart from the rudimentary (but very useful) capabilities of the LATEX picture environment and similar packages [3]. As an de facto standard for the inclusion of more complex graphics has emerged the inclusion of PostScript³ files. The complete document can then be printed on any PostScript device.

Still there are areas, where complementary approaches seem worth pursuing. In particular this is the case, if the graphical information is highly formalized, like the case at hand. Feynman diagrams are specified by their topology and the type of particles connecting the vertices. Thus a given diagram can be reproduced from a very concise specification, if the software is able to choose a reasonable layout (semi-)automatically.

 $METAFONT^{4}$ [4] and $METAPOST^{5}$ [5] appear to be the perfect tool for such a purpose, since

- 1. METAFONT is part of any (reasonable) TEX installation, thus available to all potential users,
- 2. both have very powerful graphics primitivs, which allow high quality output, and
- 3. both have builtin linear algebra, which allows us to choose a layout automatically.

Still, providing at least the basic interface in IATEX macros seems appropriate for boosting the acceptance among the less technically oriented parts of the audience. Thus feynMF⁶ [6, 7] was conceived.

feynMF is unique among packages for drawing Feynman diagrams in *combining* the following features:

• Simplicity and conciseness for common diagrams. E.g. the scattering diagram in figure 1 can be specified *completely* in five lines of LAT_FX:

 $^{2}IAT_{EX}$ might be a trademark of Addison Wesley Publishing Company.

⁵John Hobby's METAPOST is a modified version of METAFONT which generates (encapsulated) PostScript output. METAPOST can be build trivially on top of the web2c version of TEX and METAFONT for UNIX. Ports to other systems should be simple.

 $^{^{1}\}mathrm{T}_{\mathrm{E}}\mathrm{X}$ is a trademark of the American Mathematical Society.

³PostScript is a trademark of Adobe Systems Inc.

 $^{^4\}mathsf{METAFONT}$ is a trademark of Addison Wesley Publishing Company.

⁶feynMF is not anybody's trademark.



Figure 1: Simple scattering diagram.

```
\begin{fmfgraph*}(40,30) \fmfpen{thick}
  \fmfleft{i1,i2} \fmfright{o1,o2}
  \fmf{fermion}{i1,v1,o1} \fmf{fermion}{i2,v2,o2}
  \fmf{photon,label=$q$}{v1,v2} \fmfdot{v1,v2}
  \end{fmfgraph*}
```

- Expressiveness for complicated diagrams (see the examples below).
- Extensibility (e.g. see section 2.8.1).
- Arbitrary T_EX -labels. This point is more important than it may seem at first glance because most graphical layout systems lack the power to produce complicated mathematical expressions. Having matching fonts in text, equations and diagrams is also an important esthetical feature.

1.2 Relation to similar packages

Before we start, a couple of words about some complementary packages on the market are in order:

- Michael Levine's feynman package [8] is implemented on top of the standard LATEX picture environment [2]. This makes it completely portable (no need for a correct METAFONT installation), but it requires manual layout and the graphics output is (though very useful) less than perfect.
- Jos Vermaseren's axodraw package [9] uses \specials to access PostScript primitives for drawing diagrams. This approach is inherently not portable (the ubiquity of PostScript printers makes this a minor point, though) but as flexible as the present one. Nevertheless, it still requires manual layout for all diagrams.
- Last, but not least, I have to mention Thomas Leathrum's mfpic [10], which provided the inspiration for moving feynMF's user interface from METAFONT to T_EX. It might not have been unreasonable to design and implement feynMF as a package on top of mfpic, but closer inspection shows that feynMF and mfpic are fairly orthogonal. mfpic is most useful for handling simple graphical building blocks in formally unconstrained contexts. feynMF on the other hand excels in the formal context of Feynman diagrams (or any other labeled graphs for that matter), which can be drawn automatically from a *specification*.

1.3 Historical note

Parts of this code have a rather long history⁷. Some of the drawing primitives started in 1989 as feynman.mf, a library of METAFONT macros for drawing Feynman diagrams in my thesis. The layout had to be specified completely by hand, which required a long edit-process-preview cycle and made feynman.mf awkward to use. Nevertheless, it suited my and other's neeeds and survived for five years without major modifications. Early in 1994, I became aware of Thomas Leathrum's mfpic [10]. This inspired me to shift the user interface from METAFONT to LATEX, because this allows a smoother blending of the LATEX picture environment with feynMF for the purpose of labeling the graphs. While doing this and after having been taught by Tim Stelzer's and Bill Long's MADGRAPH [11] that simply minimizing the length of the graph gives much better results than I had anticipated, I added the graph manipulation and layout code.

1.4 Architecture

Even though there has never been a proper design phase in the development of feynMF, a certain structure has emerged, which is depicted in figure 2. A user who is aware of this architecture should be able to use feynMF more effectively. The most crucial aspect of the architecture is the existence of two distinct modes with different fundamental datatypes:

- *vertex mode*, which deals with graphs as structures consisting of vertices and arcs and (almost) never deals with their physical locations.
- *immediate mode*, which deals with METAFONT paths and pairs (i.e. coordinates) and allows complete control over the physical locations.

It is of course possible to mix these modes in advanced applications. Commands are provided to translate vertices and arcs to pairs and paths and vice versa. Novice users with little experience in METAFONT programming should start with vertex mode to get their job done. Later, immediate mode can be used to create more and more complex diagrams. It is possible to create most diagrams that can actually be calculated in vertex mode. Immediate mode is most useful for extending line feynMF and for drawing diagrams with fancy decorations. A word on portability: feynMF is implemented as a LATEX package. But it should be straightforward to adapt it to other TEX macro packages because LATEX macros have been used for convenience only and can easily be replaced or provided in a compatibility package. The LATEX specific environment construct can also easily be replaced by the equivalent construct in another macro package.

1.5 Conclusion

It goes without saying that feynMF is not perfect. There might be cases where using a graphical drawing tool with a mouse can give more pleasing results in less time. But in most cases, feynMF will give satisfactory results without any fine tuning. These will be reproducible and independent from the computer it is running on.

⁷Which is a partial explanation, if not excuse, for its slightly incoherent structure.



Figure 2: Architecture of feynMF: the two modes of feynMF (immediate mode and vertex mode) both interact with ET_EX and METAFONT (or METAPOST, respectively), but operate on different data types.

Early user reponses have been very encouraging. There seems to be a relatively steep learning curve for those $I\!AT_E\!X$ users that have to find out how to run METAFONT on their systems. But once this purely technical obstacle has been surmounted, users have been enthusiatic as well about the quality of the generated graphs as about the ease of use of feynMF.

2 Usage

In addition to this manual, there exists also a concise description of feynMF in a journal article [6], as well as a three part tutorial [7].

2.1 LATEX package and environments

Instructing IAT_{EX} to use feynMF is as simple as⁸

```
\usepackage{feynmf}
```

If you have METAPOST, then you can use it alternatively by placing

\usepackage{feynmp}

in your LATEX source.⁹

\usepackage[errorstop]{feynmf}
\usepackage[scroll]{feynmf}
\usepackage[batch]{feynmf}
\usepackage[nonstop]{feynmf}

fmffile All descriptions that should go into one METAFONT file are placed inside a
fmffile environment which takes the name of the METAFONT file as an argument:

\begin{fmffile}{*METAFONT-file*}

\end{fmffile}

```
\cline documentstyle[...,feynmf209,...]{...}
```

or

```
\climitstyle[...,feynmp209,...]{...}
```

If you cannot use epsf.sty for including PostScript files, you can either hack feynmp209.sty or upgrade to $I\!AT_E\!X2e$. Please keep in mind that feynMF has been developed for $I\!AT_E\!X2e$ and the $I\!AT_E\!X$ 2.09 compatibility version will always be a retrofitted hack. I will accept bug reports for the 2.09 version, but I urge everybody to move to $I\!AT_E\!X2e$, which is the one and only supported $I\!AT_E\!X$ right now.

 $^9{\tt feyn}{\sf MF}$ understands an option pre-1.03, that is of interest for veteran users:

\usepackage[pre-1.03]{feynmf}

or

 $\ensuremath{\scale{2}}\ensuremath{\scale{2$

The purpose of this option is to enable processing of old input files (pre v1.02) that use **\noexpand** in labels. Since the method for processing these files can clash (in rare cases) with $\text{IAT}_{\text{EX}} \Sigma_{\varepsilon}$'s font loading procedure, it has been disabled by default.

⁸As given, this applies to IAT_EX. But the installation file feynmf209.ins allows to generate special versions feynmf209.sty and feynmp209.sty which are compatible with the obsolete IAT_EX version 2.09. These files are to be used as documentstyle options

Upto 255 graphs can be placed into one METAFONT file. Currently feynMF does *not* check that the 255 graph limit per file is not overrun.¹⁰ Note that the filename for the METAFONT file given in the argument of the fmffile environment *must not* be identical to the LATEX source file name, because the METAFONT .log would be overwritten and LATEX can no longer access the information in this .log file. It should be obvious that any umber of diagrams can be generated by using more than one fmffile environment with different filenames.

fmfgraph The fmfgraph environment contains the description of a single Feynman diagram which will be placed a the location of the environment. Arguments are the width and the height of the diagram, in units of \unitlength:

 $\begin{fmfgraph}(\langle width \rangle, \langle height \rangle)$

\end{fmfgraph}

This environment does *not* support labels, use fmfgraph* if your diagrams contains labels.

fmfgraph* Same as fmfgraph, but enclosed in a picture environment of the same size and supporting LATEX labels.

 $\operatorname{begin{fmfgraph*}}(\langle width \rangle, \langle height \rangle)$

\end{fmfgraph*}

\fmfframe Allows to allocate additional space around a fmfgraph*, since the labels (or the diagram itself) might overshoot:

 $fmfframe(\langle left \rangle, \langle top \rangle)(\langle right \rangle, \langle bottom \rangle) \{\langle box \rangle\}$

puts an invisible frame of the given dimensions (measured in unitlength) around $\langle box \rangle$.

2.2 Auxiliary files

feynMF needs to share information between METAFONT and IAT_EX . For this task several auxiliary files are needed. The flow of information depicted in figures 3 and 4 looks much more complicated than it is. The important feature is that there a two sets of files which can be used to distribute a document:

- 1. Iff the recipient has a working METAFONT installation (which shouldn't be a problem, except for some impoverished commercial implementations), the document can be typset from the LATEX source *alone*, by running LATEX, METAFONT and LATEX again (the latter step might have to be repeated to get cross references right).
- 2. Another possibility (which doesn't require METAFONT on the recipient's side), is to distribute the IATEX source, the tfm and gf files (or pk files respectively) along with the label files with extension tn (where n as an

 $^{^{10}}$ There is also a very primitive, but (unfortunately) popular operating system, which restricts filenames to eight characters with a three character extension. On this system, only 99 graphs can be placed into one METAFONT file because auxiliary files will not be unambiguous, if more than two digits are used.



Figure 3: Interdependency of files in a feynMF application. The arrows show which files are updated in the two IATEX passes, the METAFONT pass and the final dvi translation step.

integer). Distributing the METAFONT log files is a possible alternative for the latter, but discouraged, because these are prone to be erased accidentally.

2.3 Running METAFONT

Processing your document with LATEX will generate one or more METAFONT files, which you will have to process with METAFONT. On UNIX¹¹ systems, METAFONT is invoked as

```
mf '\mode:=(METAFONT-mode); input (METAFONT-file)'
```

from the shell. Here $\langle METAFONT-file \rangle$ is to be replaced by the name of the input file (which is determined by the argument to the fmffile environment, see section 2.1) and $\langle METAFONT-mode \rangle$ is the proper METAFONT-mode for your particular printer. Please consult your local guide or local wizards about how to run METAFONT on other systems.

 $^{^{11}\}mathrm{UNIX}$ was a trademark of UNIX Systems Laboratory, but is rum ored to have been donored to X/Open.



Figure 4: Interdependency of files in a feynMF application using METAPOST: The arrows show which files are updated in the two IAT_EX passes, the META-POST pass and the final dvi translation step.

Note that $\langle METAFONT \text{-}mode \rangle$ must be specified, otherwise METAFONT will fail or the resulting font will not be usable.¹² You can look up the correct METAFONT mode in the file modes.mf that comes with the METAFONT distribution. Among the more common laser printers are laserjet for HP Laserjets at 300dpi, ljfour for HP Laserjets at 600dpi, nexthi for NeXT laser printers at 400dpi, etc.

A non-trivial part can be instructing T_EX and your favorite dvi-driver how to find the generated tfm and gf (resp. pk) files. This is highly system dependent and can be trivial (as in the standard UNIX T_EX installations, where no further action is required) or almost impossible without system priviledges (as under MVS). Please consult your local guide or wizards on this point. See also section 2.9.2 for common problems with dvi drivers.

Some recent T_EX implementations (e.g. web2c with kpathsea version 2.6 or later) are able to generate tfm files on the fly. Using such implementations, running LATEX twice should suffice and METAFONT will be invoked automagically in the background. Note however, that the automagically invoked tools might also

 $^{^{12}\}mathrm{See}$ section 2.9.1 for the typical error message and for additional information on printer modes.

install the "fonts" corresponding to the Feynman diagrams in a system directory, where they don't belong. Adding the following lines to the maketex.site script will prevent this mishap in the teT_EX distribution for UNIX (which is derived from web2c):

```
if [ -r $KPSE_DOT/$NAME.mf ]; then
    MT_PKDESTDIR=$KPSE_DOT
    MT_TFMDESTDIR=$KPSE_DOT
    MT_NAMEPART=
fi
```

The automagic tools will also *not* notice when a diagram has changed. These problems suggest that it is a generally a good idea to invoke METAFONT explicitly, instead of relying on the automagic tools.

Running METAPOST is usually trivial, because not printer specific mode is needed:

mp (METAPOST-file)

2.4 The feynmf perl script

UNIX users will be able to take advantage of the feynmf perl script, that automates the invocation of LAT_{EX} and METAPOST. In particular it tries to guess the correct METAFONT-mode and magnification. The latter is often different from 1 in slide classes. Here is the man page of feynmf:

NAME

feynmf — Process LaTeX files using FeynMF

SYNOPSIS

feynmf [-hvqncfT] [-t tfm [-t tfm ...]] [-m mode] file [file ...] feynmf [--help] [--version] [--quiet] [--noexec] [--clean] [--force] [--notfm] [--tfm tfm [--tfm tfm ...]] [--mode mode] file [file ...]

DESCRIPTION

The most complicated part of using the **FeynMF** style appears to be the proper invocation of **Metafont**. The **feynmf** script provides a convenient front end and will automagically invoke **Metafont** with the proper mode and magnifincation. It will also avoid cluttering system font directories and offers an option to clean them.

OPTIONS

```
-h, --help
```

Print a short help text.

-v, --version

Print the version of feynmf.

-q, --quiet

Don't echo the commands being executed.

-n, --noexec

Don't execute LaTeX or Metafont.

-c, --clean

Offer to delete font files that have accidentally been placed in a system directory by the **MakeTeXTFM** and **MakeTeXPK** scripts (these scripts are run by **tex** (and **latex**) in the background). This option has only been tested with recent versions of UNIX TeX.

-f, --force

Don't ask any questions.

-T, --notfm

Don't try to prepare fake .tfm files for the first run.

-t, --tfm *tfm*

Don't try guess the names of the .tfm files to fake for the first run and use the given name(s) instead. This option can be useful if our incomplete parsing of the LaTeX input files fails.

-m mode, --mode mode

Select the METAFONT mode *mode*. The default is guessed or localfont if the guess fails.

file

Main LaTeX input files.

file ...

Other LaTeX input files that are included by the main file.

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BUGS

The preparation of .tfm files is not foolproof yet, because we can parse **TeX** files only superficially.

This script has only been tested for recent **teTeX** distributions of UNIX **TeX**, though it will probably work with other versions of UNIX **TeX**. The author will be grateful for portability suggestions, even concerning **Borg** operating systems, for the benefit of those users that are forced to live with DOS or Windows.

2.5 Vertex mode

These basic features of feynMF are (or rather "should be") available through the IAT_EX interface. No knowledge of METAFONT is necessary.



Figure 6: Straight galleries.

2.5.1 External vertices

\fmfleft \fmfright \fmfbottom \fmftop \fmfsurround

Positioning of external vertices has to done explicitely. The technical reason is that they would otherwise collapse with their neighbors, but practical reasons also suggest to give the user full control here. $\{v1\},\ldots\}$ places the vertices in the comma separated list $\langle v1 \rangle,\ldots$ equidistantly on a smooth path on the left side of the diagram. $\{mfright\{\langle v1 \rangle[,\ldots]\}\}$ does the same thing on the right. Similarly $\{mfbottom and \{mftop, while \{\langle v1 \rangle[,\ldots]\}\}$ places its arguments on smooth path surrounding the diagram.

\fmfcurved \fmfstraight a

\fmftopn

Per default, the *galleries* on which we place the external vertices are curved as in figure 5, but straight galleries are also available. The macros \fmfcurved and \fmfstraight switch between these alternatives.

\fmfsurroundn 2.5.2 Arcs and internal vertices

\fmf This is the the most frequently used macro in feynMF applications.

 $\inf \{\langle style \rangle [, \langle opt \rangle [= \langle val \rangle], \dots]\} \{\langle v1 \rangle, \langle v2 \rangle [, \dots]\}$

connects the vertices $v1, v2, \ldots$ with a line of style $\langle style \rangle$, using a set of options $\langle opt \rangle$ with (optional) value $\langle val \rangle$. If a vertex is not known yet, it is added to the diagram. Note that the actual drawing is not done immediately, because the positions can only be calculated when *all* vertices are known. The currently available styles are collected in table 1. Most names should be self explanatory and are not discussed further. The **dashes**, **dots**, **phantom** and **plain** styles can optionally be decorated with an arrow as shown above. All styles, including **curly**, **wiggly** and **zigzag**, can be doubled. But arrows are not available for the latter three, because esthetically pleasing results can not be expected. The **phantom** style is special, because it only enters the vertices and does *not* cause a line to be drawn. This is extremely useful for advanced layout features, as explained below. If you need a line styles that is not listed in table 1, see section 2.8.1 for how to define your own line styles.

Name	Example	Parameters	Aliases
curly	00000000	curly_len	gluon
dbl_curly	<u>QQQQQQQQQ</u>	curly_len	
dashes		dash_len	
dashes_arrow		dash_len	scalar
dbl_dashes	========	dash_len	
dbl_dashes_arrow		dash_len	
dots		dot_len	
dots_arrow	•••••	dot_len	ghost
dbl_dots	• • • • • • • • • • • • • • • • • • • •	dot_len	
dbl_dots_arrow	•••••	dot_len	
phantom			
phantom_arrow			
plain			vanilla
plain_arrow	►		fermion, electron, quark
dbl_plain			double
dbl_plain_arrow			double_arrow, heavy
wiggly	~~~~~~	wiggly_len	boson, photon
dbl_wiggly	~~~~~~	wiggly_len	
zigzag	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	zigzag_width	
dbl_zigzag	*****	zigzag_len	

Table 1: Available line styles

The supported options are collected in table 2^{13} Note that each of the dot separated components of the options can be abbreviated. For example, 1.d is equivalent to label.dist. The result of ambiguous matches is however undefined.

Note that because the options are separated by single commata, commata inside arguments to options (label comes to mind) have to be doubled (similar to

¹³One particulary useful further option would be smooth, allowing for several lines joined smoothly. Early experimentation has shown however, that the results are not always what one expects and that there is a lot of room for abuse.

Name	Explanation
tension	draw a tighter (> 1) or more loose (< 1)
	arc
left	draw on a halfcircle on the left
right	draw on a halfcircle on the right
straight	draw on a straight line (default)
label	$T_{E}X$ text for labeling the arc
label.side	force placement of the label on the left
	or right
label.dist	place label at a distance dist
label.pos	relative position of the label (not imple-
	mented yet!)
tag	optional tag for disambiguating arcs
width	width of the line
rubout	scale factor for crossing out lines
	(doesn't work properly for doubled lines
	yet)
foreground	foreground color (METAPOST only!)
background	background color for doubled lines
	(METAPOST only!)

Table 2: Available line options

quotes in Fortran).¹⁴

Arcs that return to their origin are allowed (I will refer to them as *tadpoles*), but some options have slightly different semantics. **tension** is here a inverse scale factor for the tadpole, whose default size is 2/3 of the average distance the neighboring vertices. If left or right are specified, they give the direction (in degrees) of the preferred gap into which the tadpole is placed. By default, the largest gap is chosen for *all* tapoles at a given vertex, which will therefore overlap. This is neither a bug nor a feature, but a limitation.

\fmfn The macro \fmfn is similar to \fmf, but

$$\inf\{\langle style \rangle |, \langle opt \rangle | = \langle val \rangle |, \dots | \} \{\langle v \rangle \} \{\langle n \rangle \}$$

connects the vertices $\langle v[1] \rangle \dots \langle v[n] \rangle$.

The macro $fmfcyclen{\langle style \rangle}{\langle v \rangle}{\langle n \rangle}$ cyclically connects the vertices $\langle v[1] \rangle \dots \langle v[n] \rangle$. fmfrcyclen operates in reverse order.

Pick up a pen of the specified size. $fmfpen{\langle weight \rangle}$ is used for changing the weight (i.e. thickness) of the lines. Predefined sizes are thin and thick.

\fmfv Declare vertices with options:

 $\inf \{\langle opt \rangle [= \langle val \rangle] [, \langle opt \rangle [= \langle val \rangle], ...] \} \{\langle v1 \rangle [, ...] \}$

This is used for adding labels to a vertex and for specifying other decoration. Supported options are collected in table 3. Here the same abbreviation mechanism as above is in effect. The available **shapes** are listed in various filling styles

\fmfcyclen \fmfrcyclen \fmfpen

16

 $^{^{14}}$ Note that, as of version 1.03, it is no longer necessary to escape TEX control sequences in arguments. Old files will continue to work, because **noexpand** is temporarily disabled.

Name	Explanation
label	T_EX text for labeling the vertex
label.angle	force placement of the label at the given
	angle from the vertex
label.dist	place label at a distance dist
decoration.shape	shape of decoration
decoration.size	size of decoration
decoration.filled	fill, shade or hatch decoration
decoration.angle	rotate decoration
foreground	foreground color (METAPOST only!)
background	background color (METAPOST only!)

Table 3: Available vertex options

in table 4¹⁵. The tilings gray10, gray25, gray75 and gray90 are available in addition to gray50. Customized tilings can be created with the METAFONT function tile_from_string. It should be noted however, that tilings are gobbling up memory at high speed and should be used with discretion. The halftones¹⁶ can be accessed by giving any number from 2 to 99, which will denote the percentage of saturation (30% and 70% here)¹⁷. Again, commata inside arguments to options have to be doubled.

\fmfblob Draw a blob of the specified diameter at the vertices. Incidentally,

 $fmfblob{\langle diameter \rangle}{\langle v1 \rangle[,...]}$

is equivalent to

 $fmfv{decor.shape=circle,decor.filled=shaded, decor.size=<math>\langle diameter \rangle$ }{ $\langle v1 \rangle$ [,...]}

\fmfdot Draw a dot at the vertices given as arguments.

 $\int \left(\frac{\langle v1}{[,...]} \right)$

is equivalent to

\fmfv{decor.shape=circle,decor.filled=full,
 decor.size=2thick}{(v1)[,...]}

\fmfvn The macro \fmfvn is similar to \fmfv, but

 $\int \frac{\langle opt \rangle [= \langle val \rangle]}{\langle opt \rangle [= \langle val \rangle], \dots} \{\langle v \rangle \} \{\langle n \rangle \}$

places the vertices $\langle v[1] \rangle \dots \langle v[n] \rangle$.

 $\label{eq:linear} $$ \int mfdotn $$ d \int mfblobn $$ are similar to the fmfdot $$ and fmfblob, $$ but fmfdotn{$$ v}} places the vertices $$ $$ v[1]$... $$ v[n]$. Analogously for $$ fmfblobn. $$$

 $^{^{15}}$ If the variable feymfwizard is true (e.g. after calling the \fmfwizard macro), it is also possible to specify any METAFONT expression that evaluates to a path. Naturally, this has to used with great care, because strange errors can be triggered by typos!

 $^{^{16}}$ METAPOST will give true halftones (if your printer supports them), while METAFONT tries to mimic them. The dithering algorithm of the latter will be improved in the future.

 $^{^{17} \}mathrm{The}$ old numeric arguments in the range $-1 \dots 1$ continue to work, but are considered obsolete.

filled=	full	empty	shaded	hatched	gray50	30	70
circle		0	\bigotimes	\otimes		\bigcirc	\bigcirc
square							
triangle		\triangle		æ			
diamond		\diamond		\diamond	\blacklozenge	\diamond	
pentagon		\bigcirc	Ø	⊗		\bigcirc	
hexagon		\bigcirc	Ø	\otimes	\bigcirc	\bigcirc	
triagram		\triangle	A	\bigstar			
tetragram	+	\diamond	\$		<	\diamond	♦
pentagram	★	ক্ষ	衣	☆	☆	☆	
hexagram	*	\$	*	*	☆	\Rightarrow	*

triacross	cross	pentacross	hexacross
\prec	Х	\times	*

Table 4: Available vertex shapes and fill styles.

2.5.3 Polygons

Complex vertices with arcs attached at the corners can be contructed with polygons, which share some characteristics with arcs and vertices. The macro

\fmfpoly Th

$$\begin{aligned} \mathsf{fmfpoly}\{\langle style\rangle[\mathsf{,}\langle opt\rangle[\mathsf{=}\langle val\rangle]\mathsf{,}\ldots]\}\{\langle v1\rangle\mathsf{,}\langle v2\rangle[\mathsf{,}\ldots]\}\end{aligned}$$

places the vertices $\langle v1 \rangle$, $\langle v2 \rangle$, ... on the corners of a regular polygon. The orientation of the polygon is fixed to be mathematically positive (i.e. counter clockwise). Note that this can have strange results if the orientation is opposite to the orientation of the vertices the corners are connected to. The available options are collected in table 5. The effects of some options are depicted in table 6.

Note that is is technically *impossible* to fix the size of a polygon. The size can be controlled by specifying a **tension** for the edges, which acts like the **tension** of normal arcs.

\fmfpolyn The macro \fmfpolyn{ $\langle style \rangle$ }{ $\langle v \rangle$ } is similar to \fmfpoly but connects \fmfpolyn the vertices $\langle v[1] \rangle \dots \langle v[n] \rangle$. \fmfrpolyn operates in reverse order.

Name	Explanation
filled	fill, shade or hatch interior
phantom	don't draw anything
empty	draw outline
shade	shade interior
hatched	hatch interior
full	fill interior
pull	pull edges in (< 0) or out (> 0)
tension	tension of the edges
smooth	draw smoth corners
label	T_EX text for labeling the polygon
label.angle	force placement of the label at the given
	angle from the vertex
label.dist	place label at a distance dist
foreground	foreground color (METAPOST only!)
background	background color (METAPOST only!)

Table 5: Available polygon options

2.5.4 Color

If METAPOST is used for rendering the diagrams, vertices and arcs can be colored. The corresponding options give a warning message under METAFONT and are otherwise ignored.

Two colors are available for vertices and arcs: foreground and background. Both can either be specified as a linear combination of the predefined colors white, black, red, green and blue or as RBG triples ($\langle red \rangle, \langle green \rangle, \langle blue \rangle$). Note that as always commata have to be doubled in option arguments. Therefore both foreground=(1,,0,,1) and foreground=red+blue are valid options setting the foreground color to magenta. For arcs, the background color is used only for the interior of doubled lines.

While the color feature is rarely used in papers or books, it can be very useful for jazzing up your transparencies. See page 27 for a not very serious example.

2.5.5 Examples

After the main features of the vertex mode have been introduced, it is time for a couple of illustrative examples that are taken from *The Real World*.

As a first example, consider drawing a straightforward box diagram, familiar from $K-\bar{K}$, $D-\bar{D}$, and $B-\bar{B}$ mixing. The commands for the labels are not shown here, they are discussed in section 2.5.6

Let us start the diagram and pick up a thick pen:

```
\begin{fmfgraph}(40,25)
  \fmfpen{thick}
```

pull=	0.75	1.0	?	1.5
default				
smooth				
default	X	×	×	
smooth	-		×	
default	×			
smooth	- Alton			

Table 6: Some of the available polygon shapes. Note that pull=1.0 is identical to pull=? for straight lines, but very different for smooth lines.

The incoming and outcoming vertices are placed on the left and right hand side, respectively:

\fmfleft{i1,i2}
\fmfright{o1,o2}

Now we tell feynMF how the arcs are connected.

```
\fmf{fermion}{i1,v1,v3,o1}
\fmf{fermion}{o2,v4,v2,i2}
\fmf{photon}{v1,v2}
\fmf{photon}{v3,v4}
```

Finally we tell feynMF to draw dots at the vertices and we're done.

\fmfdotn{v}{4} \end{fmfgraph}





With a little effort the layout of this diagram can actually be improved by enlarging the inner box, see page 29 below.

Here is the resonant s-channel contribution to $e^+e^- \rightarrow 4f$. (From now on, we do no longer display the

```
\begin{fmfgraph}(40,25)
  \fmfpen{thick}
    ...
\end{fmfgraph}
```

environment surrounding all pictures.)





And the resonant *t*-channel contribution:



Two point loop diagrams pose another set of problems. We must have a way of specifying that one or more of the lines connecting the two vertices are *not* connected by a straight line. The options left, right and straight offer the possibility to connect two vertices by a semicircle detour, either on the left or on the right. Since by default all lines contribute to the tension between two vertices, the tension option allows us to reduce this tension. The next examples shows both options in action. The lower fermion line is given an tension of 1/3 to make is symmetrical with the upper line with consists of three parts. The loop photon is using a detour on the right and does not contribute any tension.

\fmfleft{i1,i2}
\fmfright{o1}
\fmf{fermion,tension=1/3}{i1,v1}
\fmf{plain}{v1,v2}
\fmf{fermion}{v2,v3}
\fmf{photon,right,tension=0}{v2,v3}





 $fmf{plain}{v3,i2} \fmf{photon}{v1,o1}$

The optional argument to left and right can be used to deform the corresponding contour as in the following example. The default value of left and right is 1.

```
\fmfleft{i} \fmfright{o}
\fmf{plain}{i,v1} \fmf{plain}{v2,o}
\fmf{dots,left=.5,tension=0.3}{v1,v2,v1}\fmffreeze
\fmf{plain,left}{v1,v2,v1}
\fmf{dashes,left=1.5}{v1,v2,v1}
```

Polygons are particulary useful for depicting non-perturbative contributions:





To conclude this first picture show, here's a self energy in scalar ϕ^4 -theory showing the simplicity of the tadpole feature:

\fmfpen{thick}
\fmfleft{i}
\fmfright{o}
\fmf{plain}{i,v,v,o}
\fmfdot{v}

Scalar $\phi^6\text{-theory}$ needs a little manual intervention to force the second on the opposite side:



\fmfpen{thick}
\fmfleft{i}
\fmfright{o}
\fmf{plain}{i,v,v,o}
\fmf{plain,left=90}{v,v}
\fmfdot{v}

2.5.6 Labels

Let us now come back to the examples on page 21 and discuss how to add the labels.

\fmflabel The macro

 $fmflabel{\langle label \rangle}{\langle v \rangle}$

is equivalent to

 $fmfv{label=\langle label \rangle}{\langle v \rangle}$

and adds the label $\langle label \rangle$ to the vertex $\langle v \rangle$. In the current implementation, there can be only a single label for each vertex. Thus earlier calls to \fmflabel for the same vertex will be overwritten. $\langle label \rangle$ will be placed with the \put command of the LATEX picture environment.¹⁸ Note that the fmfgraph* environment must be used to use labels, they will silently disappear in fmfgraph.

\fmflabel gives the user *no* control on the placement of the the label (use the \fmfv macro for a more fine-grained control). The label is placed using the following algorithm:

- 1. The reference point of the box containing $\langle label \rangle$ is placed at the distance **3thick** on the continuation of the straight line connecting the center of the picture with the vertex $\langle v \rangle$.
- 2. The reference point of the box is chosen such that the contents of the box is on the outside of the vertex (with respect to the center of the diagram). It is chosen from the four corners and the four midpoints of the sides.

Therefore the four external particles in the $B-\bar{B}$ mixing diagram on page 21 are labelled simply by:

\fmflabel{\$\bar{b}\$}{i1}
\fmflabel{\$d\$}{i2}
\fmflabel{\$\bar{d}\$}{o1}
\fmflabel{\$b\$}{o2}

 v_2

 v_8

Here is a more systematical demonstration of the default placement of labels:



\fmfsurroundn{v}{8}\fmfdotn{v}{8} \fmflabel{\$v_1\$}{v1} \fmflabel{\$v_2\$}{v2} \fmflabel{\$v_3\$}{v3} \fmflabel{\$v_4\$}{v4} \fmflabel{\$v_5\$}{v5} \fmflabel{\$v_6\$}{v6} \fmflabel{\$v_7\$}{v7} \fmflabel{\$v_8\$}{v8}

 18 Note again that, as of version 1.03, it is no longer necessary to escape T_EX control sequences in arguments. Old files will continue to work, because **noexpand** is temporarily disabled.

And here is a demonstration of the explicit placement of labels¹⁹:

		\fmfiv{d.sh=circle,d.f=1,d.si=2thin}{c}
		\fmfiv{l=-120,l.a=-120,l.d=.2w}{c}
120	60	\fmfiv{l=-60,l.a=-60,l.d=.2w}{c}
		\fmfiv{l=0,l.a=0,l.d=.2w}{c}
180 •	0	\fmfiv{l=60,l.a=60,l.d=.2w}{c}
		\fmfiv{l=120,l.a=120,l.d=.2w}{c}
-120	-60	\fmfiv{l=180,l.a=180,l.d=.2w}{c}

There is no equivalent to \fmflabel for arcs. Here options to the \fmf command have to be used. The default placement rules put the label on the outside at the midpoint of a curved arc. If the arc is straight, one should use the label.side option to push the label either to the left or to the right. This label.dist option is treated analogously to same option for vertices.

Therefore the four internal particles in the B-B mixing diagram on page 21 are labelled simply by adding options to the \fmf commands:

2.5.7 Manipulating the layout

The automatic layout algorithms of **feynMF** are rather simple, therefore it is sometimes necessary to allow for manual intervention from time to time.

- \fmffreeze Calculate the positions of the vertices based on the arcs which are defined up to this point. Usually this calculation is performed automatically at the end of the fmfgraph environment. Calling it explicitely is useful for later adding arcs that should not enter the calculation. The layout is chosen to minimize the overall length of all arcs. The length of each arc is weighted with the tension option, whose default value is 1. See section 2.5.8 for more information on \fmffreeze.
- \fmfforce $\langle pos \rangle \{ \langle v1 \rangle [, ...] \}$ forces the position $\langle pos \rangle$ of the vertices $\langle v1 \rangle ...,$ bypassing and overwriting the automatic layout. In all arguments that are METAFONT pairs (i.e. points), you can use the variable w and h, which are predefined to the width and the height of the whole diagram respectively. E.g. the center is specified as (.5w, .5h) and the lower right corner as (w, 0). The center and the four corners of the current subgraph (see the fmfsubgraph environment on page 29) are available as c, nw, ne, sw and se (for *north-west* etc).
- $\begin{aligned} & \texttt{fmfshift} \quad \texttt{fmfshift}(dist) \{ \langle v1 \rangle [, ...] \} \text{ shifts the position of the vertices } \langle v1 \rangle ... \text{ by} \\ & \langle dist \rangle \text{ from the automatic layout. This command is only useful after a } \\ & \texttt{fmffreeze} \text{ of the corresponding vertex.} \end{aligned}$
- $fmffixed \{ \langle dist \rangle \} \{ \langle v1 \rangle [, ...] \}$ fixes the distance between subsequent vertices in the list $\langle v1 \rangle$... to $\langle dist \rangle$. This command should be used with care, because

¹⁹Don't be confused by the fmfiv command. It is described below (see section 2.7.2) and takes the same arguments as the fmfv command. We use it here for convenience to place multiple vertices at the same point, i.e. the center.

it is possible to overconstrain the layout of the graph and the error messages will be obscure for a novice user.

\fmffixedx \fmffixedy $\inf_{dx} \{\langle dx \rangle\} \{\langle v1 \rangle [,...]\}$ is identical to $\inf_{dx} \{\langle dx \rangle, whatever\} \{\langle v1 \rangle [,...]\}$ and $\inf_{dy} \{\langle dy \rangle\} \{\langle v1 \rangle [,...]\}$ is identical to $\inf_{dy} \{\langle dy \rangle\} \{\langle v1 \rangle [,...]\}$. These commands can be used to fix relative positions in one coordinate, while allowing movement in the other coordinate.

2.5.8 Skeletons

The single most powerful concept for adjusting feynMF's layout decisions is the use of *skeletons*. By issuing a fmffreeze after specifying a subgraph (skeleton), we can fix the location of the skeleton *as if* the other arcs were not there. We can then successively add more subgraphs whose layout will be chosen with the skeleton remaining fixed. Similar effects can be achieved by giving some arcs a vanishing tension.

Consider the following example: suppose we want to draw a ladder diagram contributing to the quark form factor. Simply linking in the gluons does not produce a satisfactory result:

```
\fmfleft{i1} \fmfright{01,02}
\fmf{photon}{i1,v4}
\fmf{quark}{01,v1,v2,v3,v4,v5,v6,v7,o2}
\fmf{gluon}{v1,v7}
\fmf{gluon}{v2,v6}
\fmf{gluon}{v3,v5}
```

What went wrong? Obviously the gluons are bonding the quark lines too strongly. The fix is simple: just create a skeleton excluding the gluons

```
\fmfleft{i1} \fmfright{01,02}
\fmf{photon}{i1,v4}
\fmf{quark}{01,v1,v2,v3,v4,v5,v6,v7,o2}
```

and add the gluons later:

```
\fmfleft{i1} \fmfright{01,02}
\fmf{photon}{i1,v4}
\fmf{quark}{01,v1,v2,v3,v4,v5,v6,v7,o2}
\fmffreeze
\fmf{gluon}{v1,v7}
\fmf{gluon}{v2,v6}
\fmf{gluon}{v3,v5}
```

Alternatively, we can use a vanishing tension, which will effectively exclude the gluons from the layout decisions:

```
\fmfleft{i1} \fmfright{01,02}
\fmf{photon}{i1,v4}
```



```
\fmf{quark}{o1,v1,v2,v3,v4,v5,v6,v7,o2}
\fmf{gluon,tension=0}{v1,v7}
\fmf{gluon,tension=0}{v2,v6}
\fmf{gluon,tension=0}{v3,v5}
```

Which method is more intuitve is largely a matter of taste and at the discretion of the user.

The "crossed" version of this diagram is best drawn using the **rubout** option:

```
\fmfleft{i1} \fmfright{o1,o2}
\fmf{photon}{i1,v3}
\fmf{quark}{o1,v1,v2,v3,v4,v5,o2}
\fmffreeze
\fmf{gluon}{v1,v4}
\fmf{gluon,rubout}{v2,v5}
```

If rubout is selected, it defaults to 2, but it can be changed to any (reasonable) value > 1. The current implementation should work for almost all user-defined line styles. However, it does not work correctly for the predefined double line styles yet.

Another instructive example is the following: imagine you want to draw a typical non-resonant contribution to $e^+e^- \rightarrow 4f$. The obvious solution doesn't look right:





\fmfleft{i1,i2}
\fmfright{o1,o2,o3,o4}
\fmf{fermion}{i1,v1,i2}
\fmf{boson}{v1,v2}
\fmf{fermion}{o1,v2,v3,o4}
\fmf{boson}{v3,v4}
\fmf{fermion}{o3,v4,o2}

Again, we should start with a skeleton

```
\fmfleft{i1,i2}
\fmfright{01,02,03,04}
\fmf{fermion}{i1,v1,i2}
\fmf{boson}{v1,v2}
\fmf{fermion}{o1,v2,v3,o4}
```

and add the second \boldsymbol{W} later:

```
\fmfleft{i1,i2}
\fmfright{01,02,03,04}
\fmf{fermion}{i1,v1,i2}
\fmf{boson}{v1,v2}
\fmf{fermion}{01,v2,v3,04}
```



\fmffreeze
\fmf{boson}{v3,v4}
\fmf{fermion}{o3,v4,o2}

Here's another example that uses stretchable arcs. Diagrams of this kind are known as *rainbow* diagrams. If you're using METAPOST and are watching this on a color device, you'll see why.

Experience has shown that the method advocated in this section is more effective than fuzzing around with fractional tension parameters. Using \fmfshift or \fmfforce should be a last resort only.

2.5.9 Pulling strings

If you add to any arc one or more phantom arcs they will cause a tighter bonding between the vertices involved

 $\inf\{fermion\}\{v1,v2\}$

which is equivalent to

 $fmf{fermion,tension=2}{v1,v2}$

The phantom arc has to be added *before* any \fmffreeze involving these vertices, of course.

Here is an example from deep inelastic scattering²⁰:

\fmfleft{ip,il}
\fmfright{oq1,oq2,d1,oq3,d2,d3,ol}
\fmf{fermion}{ip,vp,vq,oq3}

²⁰Don't be confused by the fmfi command. It is described below (see section 2.7.1) and takes the same arguments as the fmfv command. We use it here for adding to more lines parallel to the incoming proton line. They do not enter the layout decisions.



```
\fmf{fermion}{vp,oq1}
\fmf{fermion}{vp,oq2}
\fmf{photon}{v1,vq}
\fmf{fermion}{i1,v1,o1}
\fmfblob{.15w}{vp}
\fmfdot{vq,v1}
\fmffreeze
\fmfi{plain}{vpath (__ip,__vp) shifted (thick*(0,2))}
\fmfi{plain}{vpath (__ip,__vp) shifted (thick*(1,-2))}
```

As it stands, all vertices come out too far to the right, because the greater number of outgoing lines pulls them over. Adding \fmf{phantom} makes the bond between the incoming vertices and the interactions tighter and produces a better balanced picture:

```
\fmfleft{ip,il}
\fmfright{oq1,oq2,d1,oq3,d2,d3,ol}
\fmfffermion}{ip,vp,vq,oq3}
\fmf{fermion}{ip,vp}
\fmf{fermion}{vp,oq1}
\fmfffermion}{vp,oq2}
\fmffphoton}{vl,vq}
\fmfffermion}{il,vl,ol}
\fmfflob{.15w}{vp}
\fmfdot{vq,vl}
\fmffreeze
\fmfi{plain}{vpath (__ip,__vp) shifted (thick*(0,2))}
\fmfi{plain}{vpath (__ip,__vp) shifted (thick*(1,-2))}
```

Equivalently, we could add tension to the lines in question and we will get the same result:

```
\fmfleft{ip,il}
\fmfright{oq1,oq2,d1,oq3,d2,d3,ol}
\fmf{fermion,tension=2}{ip,vp}
\fmf{fermion}{vp,vq,oq3}
\fmf{fermion}{vp,oq1}
\fmf{fermion}{vp,oq2}
\fmf{fermion}{vl,vq}
\fmfffermion,tension=2}{il,vl}
\fmfffermion}{vl,ol}
\fmffblob{.15w}{vp}
\fmfdot{vq,vl}
\fmffreeze
\fmfi{plain}{vpath (__ip,__vp) shifted (thick*(0,2))}
\fmfi{plain}{vpath (__ip,__vp) shifted (thick*(1,-2))}
```





Reconsider the box graph on page 20 and reduce the tension on the inner $lines^{21}$

```
\fmfleft{i1,i2}
fmflabel{}bar{b}}{i1}
fmflabel{$d$}{i2}
\fmfright{o1,o2}
fmflabel{}bar{d}}{01}
fmflabel{b}{o2}
fmf{fermion}{i1,v1}
\fmf{fermion,tension=.5,label=$\bar{t},,\bar{c},,\bar{u}$,
            l.side=right}{v1,v3}
fmf{fermion}{v3,o1}
fmf{fermion}{o2,v4}
\fmf{fermion,tension=.5,label=$t,,c,,u$,l.side=right}{v4,v2}
fmf{fermion}{v2,i2}
\fmf{photon,tension=.2,label=$W^+$,l.side=left}{v1,v2}
\fmf{photon,tension=.2,label=$W^-$,l.side=right}{v3,v4}
fmfdotn{v}{4}
```

This result is much nicer than the original.

$\mathbf{2.6}$ Miscellaneous commands

2.6.1Graphs in graphs

```
fmfsubgraph
```

t, c, u

 $\bar{t}, \bar{c}, \bar{u}$

b

 \overline{d}

d

 W^+

The fmfsubgraph environment contains a subgraph, for which the galleries will be placed inside the rectangle of width $\langle width \rangle$ and height $\langle height \rangle$, with lower left corner at $(\langle x \rangle, \langle y \rangle)$:

```
\operatorname{begin}\{\operatorname{fmfsubgraph}\}(\langle x \rangle, \langle y \rangle)(\langle width \rangle, \langle height \rangle)
          \langle body \rangle
\end{fmfsubgraph}
```

The center and four corners are available as c, nw, ne, sw and se (for north-west etc). Because of the restrictions on the overall size of the diagram in META-FONT, this environment will, mainly be useful for preparing transparencies with METAPOST.

Here is a not very serious application of this feature:

```
\def\subgraphsample#1{%
 fmfleftn{#1i}{2}%
 fmfrightn{#10}{2}%
 fmf{plain}{#1i1,#1v1}%
 fmf{plain}{#101,#1v2}%
 \fmf{plain}{#1o2,#1v3}%
 fmf{plain}{#1i2, #1v4}%
 fmfcyclen{plain,tension=0.3}{#1v}{4}
\begin{fmfgraph}(40,30)
 \subgraphsample{a}
```

²¹Now that you know, I have also displayed the label options used.



```
\begin{fmfsubgraph}(.3w,.3h)(.4w,.4h)
   \subgraphsample{b}
  \end{fmfsubgraph}
  \begin{fmfsubgraph}(.45w,.45h)(.1w,.1h)
    \subgraphsample{c}
  \end{fmfsubgraph}
```

More serious applications will use this feature to group together related diagrams and use other METAFONT drawing commands for graphical elements that are not available in the LATEX picture environment.

2.6.2 Reusing diagrams

\fmfkeep \fmfreuse After saving a pointer with $fmfkeep{\langle name \rangle}$ inside a fmfgraph or fmfgraph* environment, the diagram can be reused later by $fmfreuse{\langle name \rangle}$. This works across fmffile environments.

Here's an example that uses centered **\parbox**es to place diagrams into equations. The celebrated cancelation of quadratic divergencies in scalar selfenergies in supersymmetric field theories can be written as:

```
\begin{eqnarray}
\parbox{20mm}{\begin{fmfgraph}(20,15)\fmfkeep{boson}
    \fmfleft{i} \fmfright{o} \fmf{dashes}{i,v,v,o}
    \end{fmfgraph} & \propto & \Lambda^2 \\
    \parbox{20mm}{\begin{fmfgraph}(20,15)\fmfkeep{fermion}
        \fmfleft{i} \fmfright{o} \fmf{dashes}{i,v1} \fmf{dashes}{v2,o}
        \fmfleft{i} \fmfright{o} \fmf{dashes}{i,v1,v2,v1}
        \end{fmfgraph} & \propto & \Lambda^2 \\
        \parbox{20mm}{\fmfreuse{boson}} \quad + \quad
        \parbox{20mm}{\fmfreuse{fermion}} & \propto & \ln\Lambda^2
    }
}
```

The result is:

 $\propto \Lambda^2$ (1)

$$-- \bigcirc - \propto \Lambda^2$$
 (2)

2.6.3 Grouping

fmfgroup Make the enclosed \fmfset assignments local to this environment.

Parameter	Default	Semantics
thin	1pt	thin arcs
thick	1.5 thin	thicker arcs
arrow_len	4mm	length of arrow head
arrow_ang	15	opening angle of arrow head
curly_len	3mm	length of one curl
dash_len	3mm	length of one dash
dot_len	2mm	distance of two dots
wiggly_len	4mm	length of one wiggle
wiggly_slope	60	inclination of wiggles
zigzag_len	2mm	length of a zig-zag period
zigzag_width	2thick	width of zig-zag lines
decor_size	$5 \mathrm{mm}$	default size of vertex decors
dot_size	4thick	diameter of dots

Table 7: Available style parameters.

2.6.4 Changing parameters

\fmfset This command can be used to change the parameters in table 7 as follows:

$fmfset{\langle parameter \rangle}{\langle value \rangle}$

Note that these parameters are not stored in the graph data structure for the individual vertices and arcs. Instead the current values at the time of \fmfdraw are used.

2.6.5 Shrinking

fmfshrink Shrink the linewidths and similar parameters in the enclosed section.

2.6.6 Debugging

\fmftrace Enable and disable tracing of the layout decisions. This is not necessarily printed in an intuitive format, but can be helpful for debugging. \fmfdisplay Enable online displays. \fmfstopdisplay will halt METAFONT everytime a graph is complete.

2.6.7 Multiple vertices and arcs

fmffor The environment

```
\label{eq:login} $$ \eqref{fmffor} {\langle var \rangle} {\langle from \rangle} {\langle step \rangle} {\langle to \rangle} $$ \eqref{eq:login} $$ \eqre
```

executes $\langle body \rangle$ multiple times, setting $\langle var \rangle$ to $\langle from \rangle$, $\langle from \rangle + \langle step \rangle$, ..., $\langle to \rangle$. An application of this above **feynMF** feature is shown in figure 7, which is generated by calling the TEX macro

```
\def\EulerHeisenberg#1{%
```



Figure 7: Higher order terms in the Euler-Heisenberg lagrangian.

```
\begin{fmfgraph}(40,25)
 \fmfpen{thick}
 \fmfsurroundn{e}{#1}
 \begin{fmffor}{n}{1}{1}{#1}
 \fmf{photon}{e[n],i[n]}
 \end{fmffor}
 \fmfcyclen{fermion,tension=#1/8}{i}{#1}
```

with the arguments 4, 6, 8, and 10, respectively. Similarly, we can draw the diagrams from many particle physics in figures 8 and 9:

```
\def\PPRing#1{%
   \begin{fmfgraph}(20,20)
    \fmfsurroundn{v}{#1}
    \fmfdotn{v}{#1}
    \fmfcyclen{fermion,right=0.25}{v}{#1}
    \fmfcyclen{fermion,left=0.25}{v}{#1}
    \end{fmfgraph}
\def\PHRing#1{%
    \begin{fmfgraph}(20,20)
        \fmfsurroundn{v}{#1}
        \fmfdotn{v}{#1}
        \fmfcyclen{fermion,right=0.25}{v}{#1}
        \fmfcyclen{fermion,right=0.25}{v}{#1}
        \fmfrcyclen{fermion,right=0.25}{v}{#1}
        \fmfrcyclen{fermion,right=0.25}{v}{#1}
        \fmfrcyclen{fermion,right=0.25}{v}{#1}
    }
}
```

2.7 Immediate mode

In addition to the automatic layout of vertices, feynMF features an immediate mode, in which feynMF's drawing commands operate directly on METAFONT's



Figure 8: Particle-particle ring diagrams



Figure 9: Particle-hole ring diagrams

pairs and paths. You might want to consult The METAFONT Book [4] or the METAPOST manual [5] for further information on the available path expressions.

2.7.1 Arcs

\fmfi Immediate mode's brother of \fmf.

$$\inf\{\langle style \rangle [, \langle opt \rangle [= \langle val \rangle], \ldots]\} \{\langle p \rangle \}$$

draws a line of style $\langle style \rangle$ on path $\langle p \rangle$. Use the vpath function in $\langle p \rangle$ (after \fmffreeze!) to access the METAFONT path connecting two vertices: vpath[$\langle tag \rangle$]($\langle from \rangle, \langle to \rangle$). The optional numeric $\langle tag \rangle$ can be used together with a matching tag option to \fmf to disambiguate arcs that connect the same vertices. You have to prepend each name of a vertex in vpath's arguments with two underscores (e.g. v1 becomes __v1). This is necessary for avoiding name-clashes with some reserved words in METAFONT (sparks in DEK's terminology).

2.7.2 Vertices

\fmfiv Immediate mode's brother of \fmfv.

$$\int \mathfrak{shape} = \langle val \rangle [\langle val \rangle] [\langle val \rangle], \dots] \{ \langle v \rangle \}$$

draws a vertex at position $\langle v \rangle$. Note that here $\langle v \rangle$ is a METAFONT pair and *not* a feynMF vertex name. The former's equivalent of the latter can be accessed (*after* \fmffreeze!) with the vloc function: vloc($\langle vertex \rangle$). Again, you have to prepend the name of the vertex in vloc's argument with two underscores (e.g. v1 becomes __v1).

2.7.3 Declarations

\fmfipath The argument(s) are declared METAFONT paths. \fmfipair The argument(s) are declared METAFONT pairs (coordinates).

2.7.4 Assignments

- \fmfiequ Establish equality for the two arguments, i.e. \fmfiequ{lval}{rval} translates to lval=rval.
- \fmfiset Assign the second argument to the first, i.e. \fmfiset{lval}{rval} translates to lval:=rval.

Specifying equality of two variables is a very different operation from assignment in METAFONT. See The METAFONT Book [4] for details on METAFONT's builtin equation solver.

2.7.5 Examples

Here is a non-trivial example of immediate mode, which shows some useful tricks. The non-trivial aspect of the diagram in question is that it has lines broken in two, denoting particles coupling to a condensate.

We start the diagram with a skeleton (the **phantom** lines are shown as thin lines for clarity):



```
\fmfleft{i}
\fmfright{o}
\fmf{dots}{i,v1}
\fmf{dots}{v2,o}
\fmf{phantom,left,tension=0.2,tag=1}{v1,v2}
\fmf{phantom,left,tension=0.2,tag=2}{v2,v1}
\fmfdot{v1,v2}
\fmfposition
```

Add the fermions to the skeleton



```
\fmfipath{p[]}
\fmfiset{p1}{vpath1(__v1,__v2)}
\fmfiset{p2}{vpath2(__v2,__v1)}
\fmfi{fermion}{subpath (0,length(p1)/3) of p1}
\fmfi{fermion}{subpath (2length(p1)/3,length(p1)) of p1}
\fmfi{fermion}{subpath (0,length(p2)/3) of p2}
\fmfi{fermion}{subpath (2length(p2)/3,length(p2)) of p2}
```

Add condensates and a gluon





Figure 10: Circular gluons.

Here's an interesting abuse of feynMF (see the next section for \fmfcmd):



Finally, for the curious, here is how to draw the circular gluons in figure 10:

```
\fmfi{gluon}{fullcircle scaled .5w shifted (.5w,.5h)}
\fmfi{gluon}{reverse fullcircle scaled .5w shifted (.5w,.5h)}
```

2.8 Raw METAFONT

Some more advanced features of feynMF are more conveniently accessed through raw METAFONT commands. This can either be achieved by preparing a METAFONT input file or by using \fmfcmd extensively. The latter apprach is usally more convenient.

\fmfcmd The \fmfcmd macro writes its argument into the METAFONT input file generated by feynMF. While some experience in using METAFONT doesn't hurt here, this approach can simplify the production of complex diagrams considerably. Note that *no* semicolon is appended, the user has to provide it explicitly.

2.8.1 Extending feynMF

A prominent example for using raw METAFONT is provided by the option to add new styles for arcs. There is of course always one more style that *must* be added to the default list. But increasing this list without bounds will eventually slow down feynMF and increase its memory requirements. It is therefore better to allow users to define their own styles. This is done with the METAFONT macro style_def, which defines a macro that will be called to do the drawing and registers this macro with feynMF so that it can be used in the first argument to \fmf.

The macro takes one argument of type **path** and is responsible for drawing the arc on this path. If METAPOST's color functionality is to be used, the color aware functions cdraw, cfill, cfilldraw, ccutdraw and cdrawdot should be used instead of draw, etc.

After the following style_def, a new style crossed will be available:

```
\fmfcmd{%
  vardef cross_bar (expr p, len, ang) =
   ((-len/2,0)--(len/2,0))
     rotated (ang + angle direction length(p)/2 of p)
     shifted point length(p)/2 of p
  enddef;
  style_def crossed expr p =
     cdraw p;
     ccutdraw cross_bar (p, 5mm, 45);
     ccutdraw cross_bar (p, 5mm, -45)
  enddef;}
```

it can be used just like any other style:

```
\fmfleft{i}
\fmfright{o}
\fmf{plain}{i,v,o}
\fmf{crossed}{v,v}
\fmfdot{v}
```

And here is an (esthetically questionable!) attempt at wiggly lines with arrows:

```
\fmfcmd{%
    style_def wiggly_arrow expr p =
    cdraw (wiggly p);
    shrink (2);
    cfill (arrow p);
    endshrink;
enddef:}
```





Note how the **shrink** macro (which is the METAFONT equivalent of the **fmfshrink** environment) is used to temporarily double the dimensions of the arrowhead which is constructed by the **arrow** macro.

In particular theorists beyond the standard model are likely to need *a lot* of different line styles. The aficionados of majorana neutrinos might find the following two useful:

```
\fmfcmd{%
  style_def majorana expr p =
    cdraw p;
    cfill (harrow (reverse p, .5));
    cfill (harrow (p, .5))
  enddef;
  style_def alt_majorana expr p =
    cdraw p;
    cfill (tarrow (reverse p, .55));
    cfill (tarrow (p, .55))
  enddef;}
```

Note the use of the harrow and tarrow functions which return an arrowhead on the given fraction of the path, with reference points at the head (harrow) or tail (tarrow). The arrow function used above is equivalent to marrow(p,.5), which has the reference point at the center of the arrowhead. Having the three different reference point available is important for supporting arcs of substantially differing lengths.

A problem of the current implementation is that the endpoints of double lines don't match smoothly at vertices:

```
\fmfpen{thick}\fmfleftn{l}{2}\fmfrightn{r}{2}
\fmfpolyn{shaded}{z}{4}
\fmf{dbl_plain_arrow}{l2,z3}
\fmf{dbl_plain_arrow}{l1,z4}
\fmf{dbl_plain_arrow}{z1,r1}
\fmf{dbl_plain_arrow}{z2,r2}
```

One way around is to add dots of the right size at the vertices *after* the arcs have been drawn.

```
\fmfpen{thick}\fmfleftn{l}{2}\fmfrightn{r}{2}
\fmfpolyn{shaded}{z}{4}
\fmf{dbl_plain_arrow}{l2,z3}
\fmf{dbl_plain_arrow}{l1,z4}
\fmf{dbl_plain_arrow}{z1,r1}
\fmf{dbl_plain_arrow}{z2,r2}
\fmffreeze\fmfdraw
\fmfvn{d.siz=2thick,d.sh=circle}{z}{4}
```





Without the fmffreeze fmfdraw, the arcs would "know" about the dots and would be shortened.

A more elegant solution is to define line styles with dots at the head,

```
\fmfcmd{vardef endpoint_dot expr p =
  save oldpen; pen oldpen;
  oldpen := currentpen;
 pickup oldpen scaled 3;
 cdrawdot p;
 pickup oldpen;
enddef;}
\fmfcmd{style_def hd_double expr p =
  draw_double p;
  endpoint_dot point infinity of p;
enddef;}
\fmfcmd{style_def hd_dbl_plain_arrow expr p =
  draw_hd_double p;
  shrink (1.5);
    cfill (arrow p);
  endshrink;
enddef;}
```

 tail

```
\fmfcmd{style_def td_double expr p =
    draw_double p;
    endpoint_dot point 0 of p;
enddef;}
\fmfcmd{style_def td_dbl_plain_arrow expr p =
    draw_td_double p;
    shrink (1.5);
    cfill (arrow p);
    endshrink;
enddef;}
```

or both

```
\fmfcmd{style_def htd_double expr p =
    draw_double p;
    endpoint_dot point 0 of p;
    endpoint_dot point infinity of p;
enddef;}
\fmfcmd{style_def htd_dbl_plain_arrow expr p =
    draw_htd_double p;
    shrink (1.5);
    cfill (arrow p);
    endshrink;
enddef;}
```

which can be used as follows to give an equivalent result:



```
\fmfpen{thick}\fmfleftn{1}{2}\fmfrightn{r}{2}
\fmfpolyn{shaded}{z}{4}
\fmf{hd_dbl_plain_arrow}{12,z3}
\fmf{hd_dbl_plain_arrow}{11,z4}
\fmf{td_dbl_plain_arrow}{z1,r1}
\fmf{td_dbl_plain_arrow}{z2,r2}
```

2.9 Common traps, trouble shooting and frequently asked questions (FAQs)

2.9.1 ! Value is too large

The following will be one of the most frequent errors:

It can have one of two causes:

- METAFONT was invoked without specifying the mode. This case is easily fixed by looking up the correct METAFONT mode in the file modes.mf that comes with the METAFONT distribution. This mode *must* be specified on the command line as \mode:=laserjet for HP Laserjets at 300dpi, as \mode:=ljfour for HP Laserjets at 600dpi, as \mode:=nexthi for NeXT laser printers at 400dpi, etc, just to name three of the more common laser printers in the physics community.
- The diagrams are too large for the printer at hand. This case is actually not very likely, because even at 1200dpi the diagrams can be as large as 86mm. For the popular laserprinter resolution of 300dpi, even 346mm are possible. Last time I checked, the diagrams for this manual could be generated for a *Linotype Linotronic 300* at 2540dpi (mode:=linosuper), but failed in the standard proof mode at 2601.72dpi.²² In fact, in the current modes.mf file, the *Chelgraph IBX* at 9600dpi and the *Alphatype CRS* at 5333 + 1/3dpi are the only typesetters that can not be used to typeset this manual.²³

 $^{^{22}}$ It would be trivial to shrink the diagrams by 1% to make them work in **proof** mode (accidentally, the largest diagram is 40mm wide, while 4096/2601.72dpi corresponds to 39.99mm). However, I prefer METAFONT to give an error message if the user forgot to specify the mode. It is much more obscure when METAFONT works without errors but the dvi driver fails to find the generated bitmap file.

 $^{^{23}}$ If someone wants to use feynMF with one of these high end typesetters, I would be glad to try to help them out with kludges.

2.9.2 Diagrams in the document are never updated

There are two known reasons why diagrams may not be updated the document after the source file has been changed:

- Some dvi file previewers (e.g. xdvi(1) under UNIX) do *not* reread font information if the tfm or pk files have changed, even though they reread the dvi file if it has changed. Therefore you have to restart such previewers if you have made changes in diagrams to see these changes on the screen.
- Some dvi drivers (e.g. dvips(1) under UNIX) do not work with the gf files directly, but convert them with an external program to pk format first. On later occasions, the dvi driver will then use the pk file which is out of date with respect to the sources and the gf file. The only known fix is to delete the pk fils before running the dvi driver.

2.9.3 Disgrams show up in the wrong spot

If you are using feynMF with LATEX's \includeonly feature, you should watch out for the following situation:

```
\includeonly{bar1,bar3}
\begin{fmffile}{foograph}
\include{bar1}
\include{bar2}
\include{bar3}
\end{fmffile}
```

where bar1.tex defines graph #1, bar2.tex graph #2 and bar3.tex defines graph #3. If you now proceeded to add graphs to bar1.tex, you will notice that a second graph is accepted, but instead of the new third graph, the old graph #3 appears. What happens is that LATEX stores the value of the counter for fmfgraphs in each .aux file so that because bar2.tex is not processed, this counter is always reset to 3 at the beginning of bar3.tex.

Even though this situation appears to be contrived, it actually occured in real life applications and the resulting error is very confusing.

The only "fix" for this problem would be to use a private counter behind LATEX's back. Unfortunately, it appears that this will violate the *principle of minimal surprise* even more. It is therefore usually a good idea to reprocess the complete document when the number of graphs has changed in an \included file. The other solution is to have a separate fmfgraph environment for each \included file.

2.9.4 Spurious labels show up

If spurious labels show up in your diagrams, this is most likely caused by old label files (e.g. foo.t $\langle n \rangle$) still lying around. Just delete these files and rerun T_EX and METAFONT (or METAPOST respectively).

2.10 Known bugs

2.10.1 Chaotic manual

This is being worked on. It should probably be rewritten from scratch, but I don't have enough time at the moment (this is a spare time activity).

2.10.2 Delayed error messages

This can't be fixed. The problem is that errors can manifest themselves only a long time after the corresponding source line has been read. Since T_EX doesn't allow to access the current source line number, there is no way to store this information along with the other information on the graph. I can only hope to have enough sanity checks in place some day that error messages from META-FONT won't occur.

2.10.3 Multiple tadpoles

Currently, feynMF will not layout multiple tadpoles at a single vertex automatically. This could be fixed in principle, but these fixes would cause other problems which are more inconvenient than having to lay out tadpoles manually.

2.10.4 Hard limits

Currently the most severe limitation lies in the size of the generated pictures. The largest number METAFONT can represent internally is 4095.99998 and this is also the largest value any coordinate measured in pixels can assume. At the most popular laserprinter resolution of 300 dots per inch (dpi), this corresponds to a horizontal and vertical extension of about 346mm, which is plenty and we're more likely to hit the internal limits on the complexity of a picture. However, at the proof mode resolution of 2601.72dpi, this is reduced to slightly less than 40mm and we're running the risk of arithmetic overflow in internal calculations much earlier.

There are two potential solutions of different scope and complexity:

- Since John Hobby's METAPOST is now available without a non-disclosure agreement from AT&T, one solution is to replace METAFONT by META-POST, which doesn't suffer from the size limitations. This comes with a small price paid in reduced portability of the generated output, but as already stated above in the case of axodraw, the ubiquity of PostScript printers (and the free GhostScript interpreter) makes this a minor point.
- The more ambitious solutions would be *virtual graphs*, i.e. graphs which are larger than the current limit enforced by numeric overflow at higher resolutions. This could be implemented by calculating the layout of a miniature graph and afterwards distributing the full graph among several METAFONT characters.

Acknowledgements

I am most grateful to Wolfgang Kilian, who pushed feynMF's predecessor feynman.mf to its limits [12]. Discussions with him triggered a lot of good

ideas. Thanks also to my students and the people on *The Net* for suggestions, portability fixes and for volunteering as guinea pigs.

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Distribution

feynMF is available by an onymous internet ftp from any of the Comprehensive T_FX Archive Network (CTAN) hosts

ftp.shsu.edu, ftp.tex.ac.uk, ttp.dante.de

in the directory

macros/latex/contrib/supported/feynmf

It is also available from the host

crunch.ikp.physik.th-darmstadt.de

in the directory

pub/ohl/feynmf

Unsupported snapshots of my work in progress are provided as

pub/ohl/feynmf.versions/feynmf-current.tar.gz

There are two mailing lists

```
feynmf-announce@crunch.ikp.physik.th-darmstadt.de
feynmf-bugs@crunch.ikp.physik.th-darmstadt.de
```

open for subscription. The former should carry only important announcements, of new versions in particular. To subscribe, send mail to the (electronic) mailing list manager

```
majordomo@crunch.ikp.physik.th-darmstadt.de
```

and *not* to the lists itself. The following commands (on a line in the body of the mail, not in the subject) are useful:

```
subscribe feynmf-announce
unsubscribe feynmf-announce
help
```

Index

Numbers written in italic refer to the page where the corresponding entry is described; numbers underlined refer to the code line of the definition; numbers in roman refer to the code lines where the entry is used.

Symbols	С	\fmf 14
-T, $-notfm@-T$,	color 19	\fmfblob 17
notfm 13	crossed arcs 36	fmfblobn 17
-c, –clean@ -c , clean 13		\fmfbottom $\dots \dots 14$
-f, -force@ -f , force 13	D	\fmfbottomn 14
-h, -help@ -h , help 12	defining new styles 36	\fmfcmd $\dots \dots 35$
-m mode, –mode	displays, online 31	\fmfcurved $\dots \dots 14$
mode@-m	dots $\dots \dots \dots \dots \dots \dots 17$	\fmfcyclen 16
mode,mode		$fmfdisplay \dots 31$
mode 13	\mathbf{E}	\fmfdot 17
-n,noexec@ -n ,	environments:	\fmfdotn 17
noexec 13	fmffile $\ldots \ldots 8$	fmffile (environ-
$-q, \qquad -quiet@-q,$	fmffor $\dots \dots 31$	ment) $\ldots \ldots 8$
quiet 13	fmfgraph9	\fmffixed $\dots \dots 24$
-t, -tfm tfm@ -t , tfm	fmfgraph* $\dots 9$	fmffixedx 25
tfm	fmfgroup 30	\fmffixedy 25
-v, $-version@-v$,	fmfshrink $\dots \dots 31$	fmffor (environment) 31
version \dots 12	fmfsubgraph \dots 29	\fmfforce $\dots \dots 24$
	extensions $\ldots \ldots 36$	$fmfframe \dots g$
\mathbf{A}	external vertices 14	\fmffreeze 24
arcs $\dots \dots 14, 16, 33$		fmfgraph (environ-
		ment) $\dots \dots g$
В	file \dots @file \dots \dots 13	
blobs 17	file@file $\dots \dots 13$	ment) $\dots \dots g$

fmfgroup (environ- ment) 30	\fmfshift 24 fmfshrink (environ-	O online displays 31
\fmfi 33	ment) $\dots \dots 31$	OPTIONS 12
\fmfiequ 34	\fmfstopdisplay 31	
\fmfipair	\fmfstraight 14	Р
\fmfipath 33	fmfsubgraph (environ-	parameters $\ldots \ldots 31$
\fmfiset	ment) $\dots \dots 29$	polygons $\dots \dots \dots 18$
\fmfiv	\fmfsurround 14	
\fmfkeep <i>30</i>	\fmfsurroundn \dots 14	R
\fmflabel 23	\fmftop 14	running METAFONT . 10
\fmfleft	$fmftopn \dots 14$	running METAPOST . 12
\fmfleftn 14	$fmftrace \dots 31$	G
\fmfn 16	\fmfv 16	S
\fmfnotrace 31	\fmfvn 17	styles, defining new 36
\fmfpen 16		subgraphs 29
\fmfpoly 18	G	m
\fmfpolyn 18	galleries 14	T
		tadpoles $\dots \dots \dots 22$
\fmfrcyclen 16	I	tracing $\ldots \ldots 31$
\fmfreuse 30	internal vertices . 16, 17	
fmfright 14		\mathbf{V}
fmfrightn 14	\mathbf{L}	vertices $\dots \dots \dots 33$
fmfrpolyn 18	labels $14, 16, 23, 24$	vertices, external 14
\fmfset 31	looping $\ldots \ldots 31$	vertices, internal . 16, 17